

# Blurring the Lines Between Assessment and Instruction

**ZACHARY CHAMPAGNE**

[zakchamp.com](http://zakchamp.com) |  [@zakchamp](https://twitter.com/zakchamp) | [zacharychampagne@gmail.com](mailto:zacharychampagne@gmail.com)



# Kids Have Important Mathematical Ideas



A diagram consisting of three large circles arranged horizontally. The leftmost circle is yellow and contains the word 'Teaching'. The middle circle is teal and contains the word 'Learning'. The rightmost circle is orange and contains the word 'Assessment'.

Teaching

Learning

Assessment





Assessment

Learning

Teaching



A large yellow circle containing the word "Teaching" in white text.

Teaching

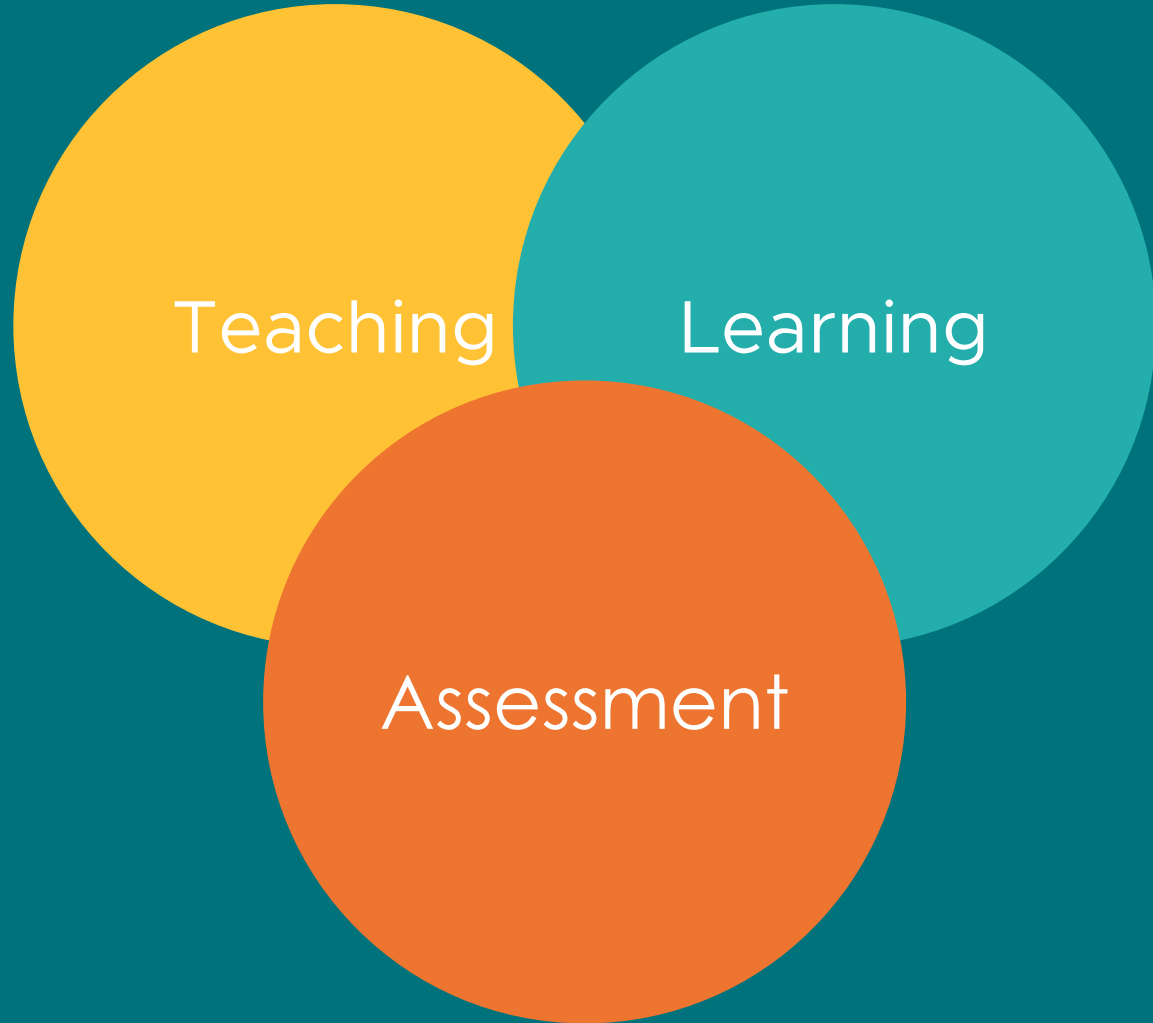
A large orange circle containing the word "Assessment" in white text.

Assessment

A large teal circle containing the word "Learning" in white text.

Learning





Teaching  
Learning  
Assessment



# When Assessing Students, What Matters?

- How they are thinking about the mathematics
- What they know and understand (rather than what they don't know)
- How it can inform our instruction
- What is their relationship with mathematics
- The wording/presentation of the task





# Consider This Task

DANIEL RODRIGUEZ QUINTANA/THINKSTOCK



Name \_\_\_\_\_

## The Cycling Shop

Imagine you work at a cycling shop building unicycles, bicycles, and tricycles for customers. One day, you receive a shipment of 8 wheels. Presuming that each cycle uses the same type and size of wheel, what are all the combinations of cycles you can make using all 8 wheels?

From the August 2016 issue of **children** teaching **mathematics**



Imagine you work at a cycling shop building unicycles, bicycles, and tricycles for customers. One day, you receive a shipment of 8 wheels. Presuming that each cycle uses the same type and size of wheels, what are all the combinations of cycles you can make using all 8 wheels?

| Unicycles | Bicycles | Tricycles | Total Wheels |
|-----------|----------|-----------|--------------|
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |



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| Unicycles | Bicycles | Tricycles | Total Wheels |
|-----------|----------|-----------|--------------|
| 8         | 0        | 0         | 8            |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |



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| Unicycles | Bicycles | Tricycles | Total Wheels |
|-----------|----------|-----------|--------------|
| 8         | 0        | 0         | 8            |
| 6         | ?        | ?         | ?            |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |
|           |          |           |              |



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$$\square + \square + \square = \square$$



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$$\square + \square + \square = 8$$



# Consider All That You Can Learn With Just a Blank Page





## Tweet

↻ Florida Department of Education Retweeted

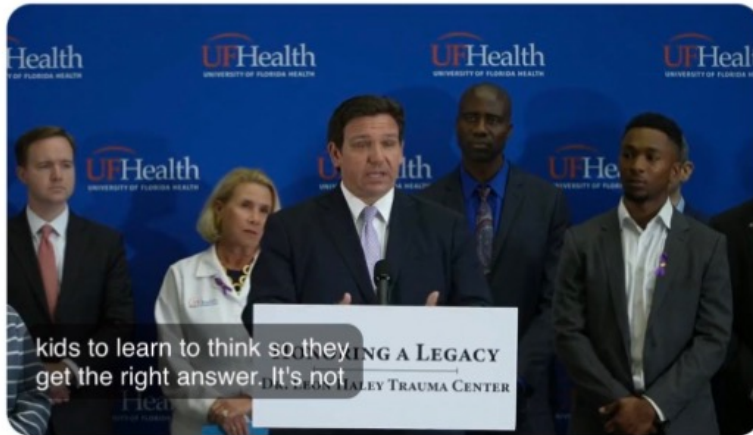


**Ron DeSantis** ✓  
@GovRonDeSantis



Math is about getting the right answer,  
not about feelings or ideologies.

In Florida, we will be educating our  
children, not indoctrinating them.



8:35 PM · Apr 20, 2022 from Florida, USA · Twitter for iPhone





# The Teaching and Learning of Mathematics is NOT About Right Answers



When my students are learning mathematics, the answer is less critical.

It only tells me one thing.

How a student arrives at that answer tells me LOTS of things.



# Story Problem Routine



Mr. Zak has 16 pieces of candy.

Ms. Claire has 9 pieces of candy.



Mr. Zak has 16 pieces of candy.  
Ms. Claire has 9 pieces of candy.

How many more pieces of candy does  
Mr. Zak have than Ms. Claire?



A farm is selling eggs by the dozen.

You buy 7 dozen eggs.



A farm is selling eggs by the dozen.

You buy 7 dozen eggs.  
How many eggs do you have?



# Let's Talk About Listening





“The best we can do as journalists is to try and listen to people. And one of the suggestions that I make - that will help unite us all - is that we take a more civil tone and to do that we need to try and listen to one another.”

-Dan Rather



Hearing is a physical process.

Listening is hearing and then actually reflecting upon what you're hearing.

Listening is a cognitive process, and it's the first step in understanding and learning.



# How Do We Become Better Listeners?

- Ask questions you don't know the answer to
- Get away from the board
- Allow for more student talk
- Provide pause



# How Do We Become Better Listeners?

- Ask questions you don't know the answer to
- Get away from the board
- Allow for more student talk
- Provide pause**



# Landon

There were 25 red apples and some green apples on the table. Together there were 51 apples on the table.  
How many were green?



# Landon

There were 25 red apples and some green apples on the table.  
Together there were 51 apples on the table. How many were  
green? = 26

$$\begin{array}{r} 25 \\ + 26 \\ \hline 51 \end{array}$$



# Landon

There were 5 baskets. Each basket had 6 crayons in it. How many crayons were there in all the baskets?



# Landon

There were 5 baskets. Each basket had 6 crayons in it. How many crayons were there in all the baskets? = 30

$$6 \times 5 = 30$$





# Landon

199 + 55



# Landon

$199 + 55 = 254$

So now I solved this  
was I had 199 dollars  
then I found 55 more  
dollars  
200 then I added  $1 + 199 =$   
254 then I added 54

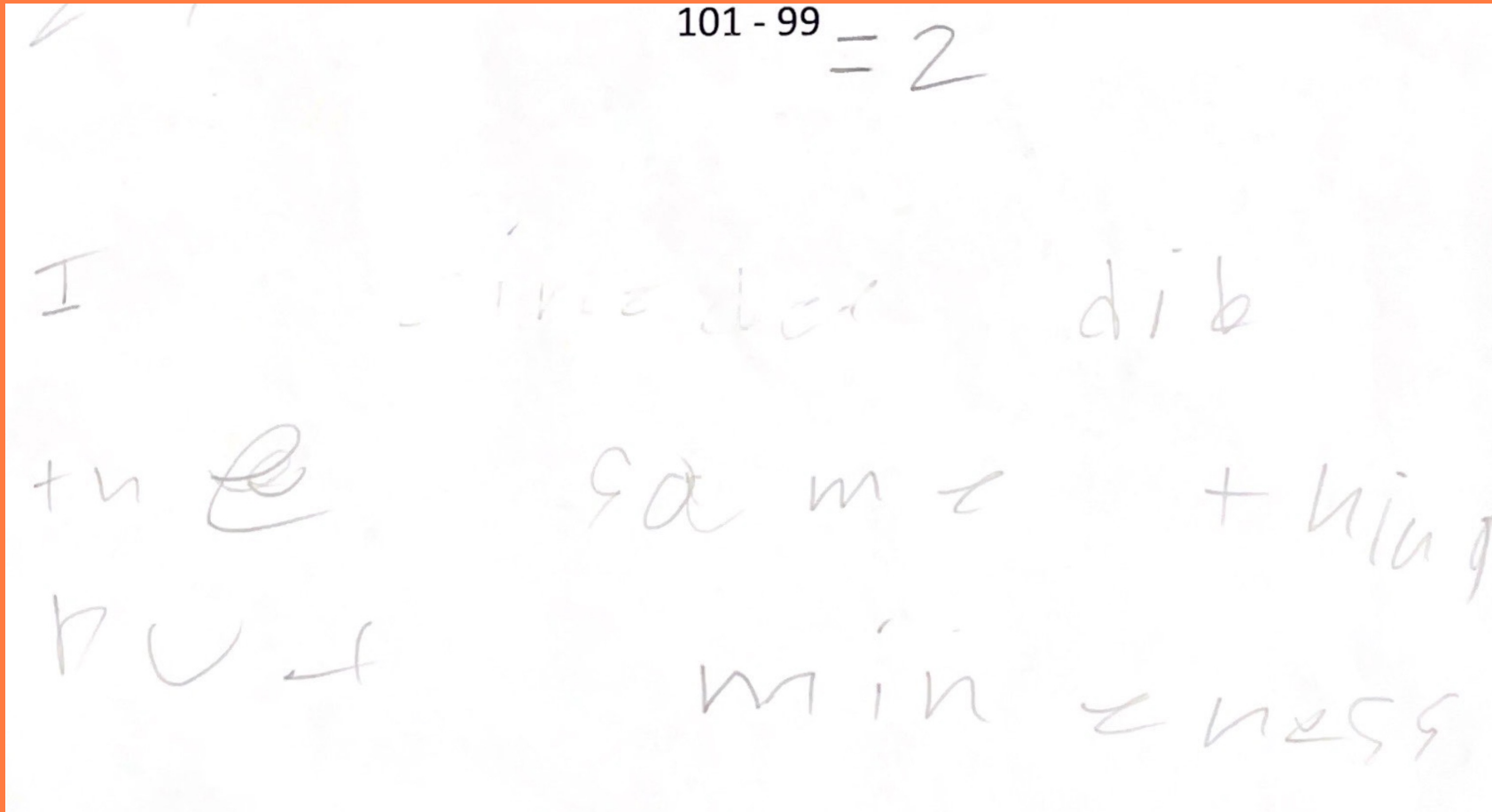


# Landon

101 - 99



# Landon



“I did the same thing but minuses”

# Gavin

A school is taking everyone on a field trip. It needs buses to transport 375 people.

Bus Company A has small buses with 27 seats in each.

Bus Company B has large buses with 48 seats in each.

What is the smallest number of buses that will be needed if the school goes with:

Bus Company A? Bus Company B? Show your reasoning.



# Gavin

A school is taking everyone on a field trip. It needs buses to transport 375 people.

Bus Company A has small buses with 27 seats in each.  
Bus Company B has large buses with 48 seats in each.

What is the smallest number of buses that will be needed if the school goes with:  
Bus Company A? Show your reasoning.

$$\begin{array}{r} 27, 54, 108, 324 \\ 1 \quad 2 \quad 4 \quad 12 \end{array} \quad \begin{array}{r} 375 \\ 14 \end{array}$$

Bus Company B? Show your reasoning.

$$\begin{array}{r} 48, 96, 390 \\ 1 \quad 2 \quad 8 \end{array}$$

Illustrative Math



# Gavin

How long to fill up the biggest pickle jar?



# Gavin

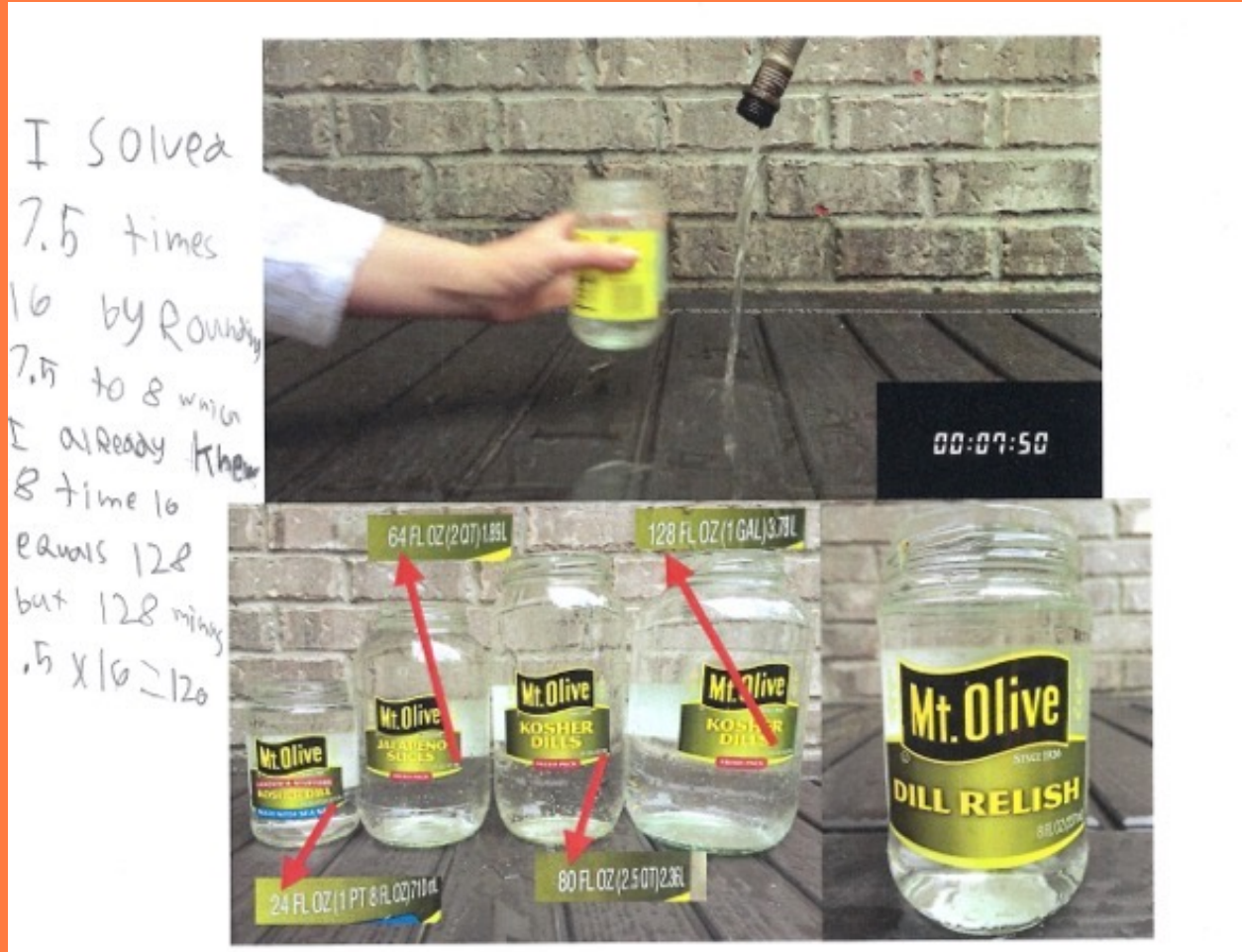
How long will it take to fill up the large jar?

I think it will take  
2 minutes to fill up the big jar  
because the little jar was 8 ounces  
and the big jar was 128 ounces so  
 $8 \times 8 = 64$   $16 \times 8 = 128$   
so 16 times  $7.50 = 120$  and  $120 \text{ seconds} = 2 \text{ min}$



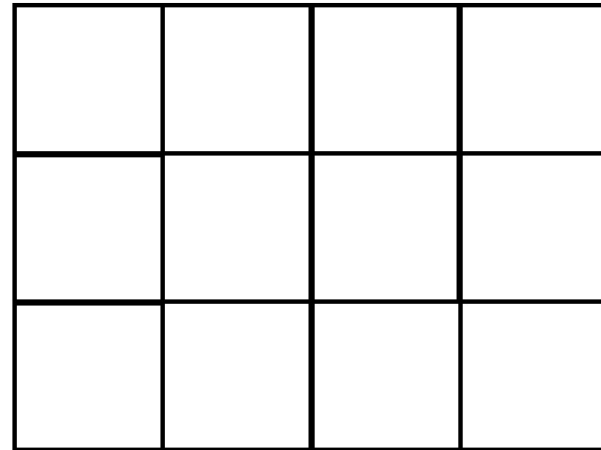
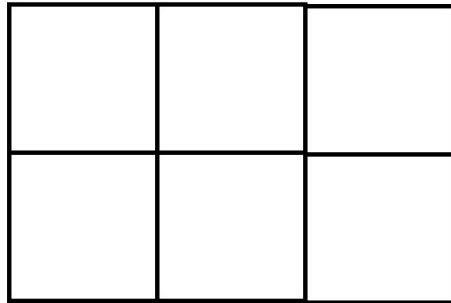
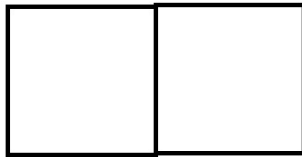


# Gavin



# G7 and G8 problem

Look at the following growing pattern below. What do you notice? What do you wonder?



Developing Mathematical Ideas



# G7 and G8 problem

Look at this table. What do you notice? What do you wonder?

| Height | Number of Tiles |
|--------|-----------------|
| 1      | 2               |
| 2      | 6               |
| 3      | 12              |
| 4      | ?               |

Developing Mathematical Ideas



# G7 and G8 problem

Continue the table up to rectangles with a height of 10.

What observations do you notice about the values in the table? How is it growing?

What would a graph for this table look like? Would it be linear? How do you know?

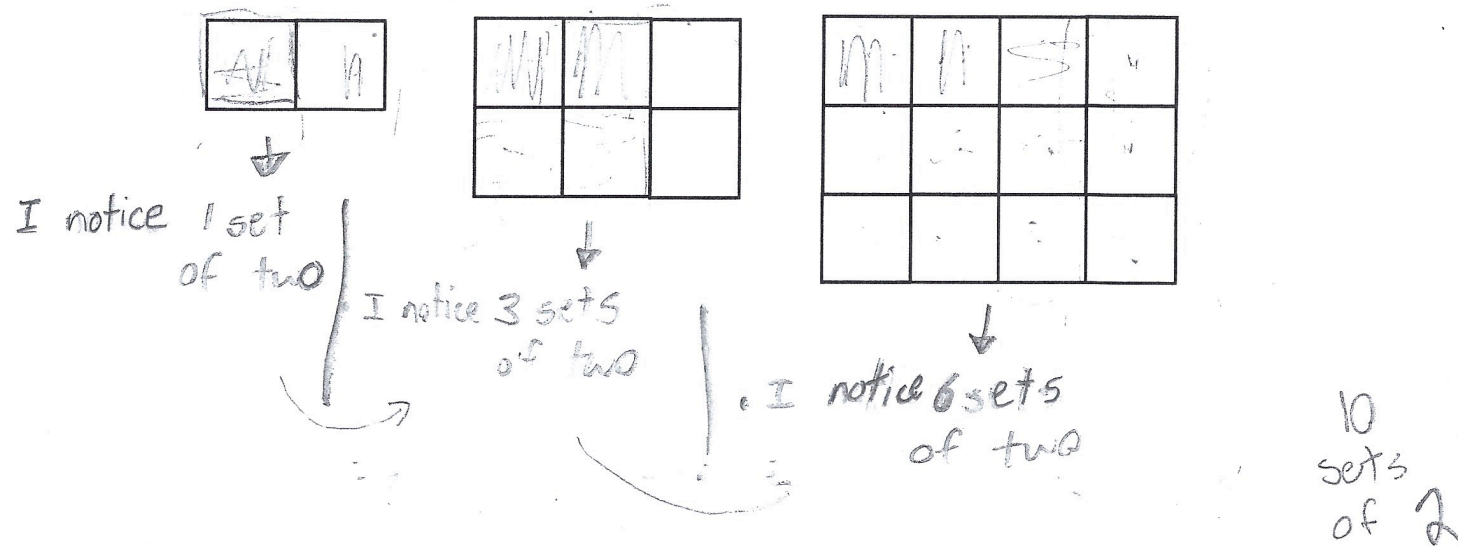
Is there a rule for this pattern? Can you write it out in words? Or as an equation?

Developing Mathematical Ideas



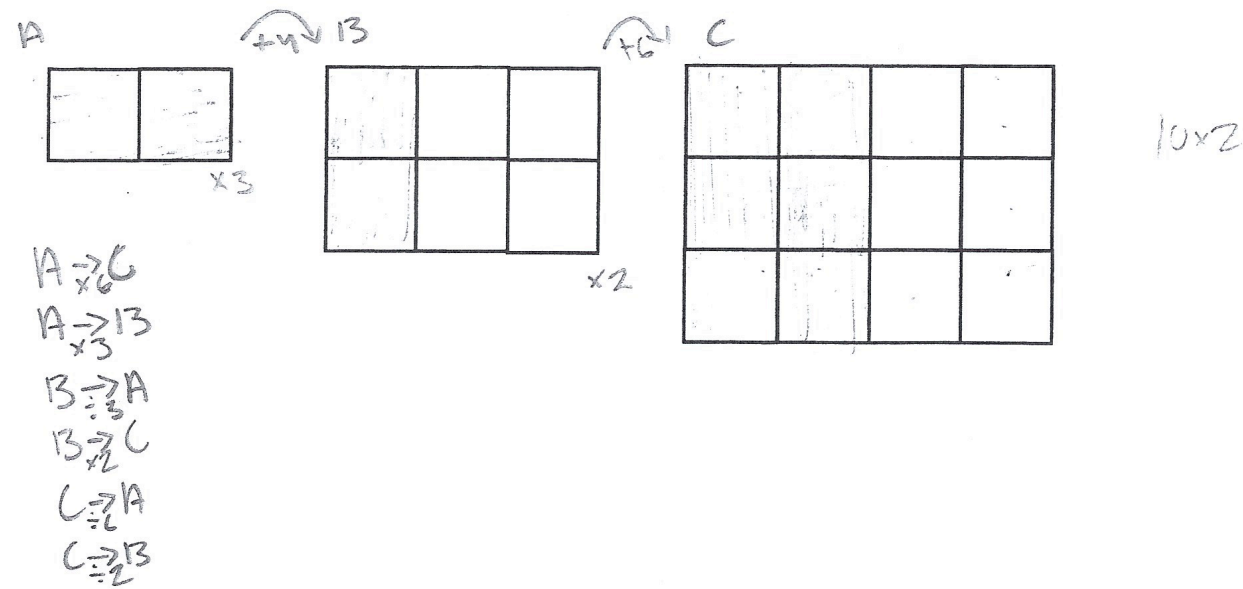
# Joy

Look at the following growing pattern below. What do you notice? What do you wonder?



# Abby

Look at the following growing pattern below. What do you notice? What do you wonder?



# Joy

Look at this table. What do you notice? What do you wonder?

| Height | Number of Tiles |
|--------|-----------------|
| 1      | 2               |
| 2      | 6               |
| 3      | 12              |
| 4      | ?               |

$$4 \times 5 = 20$$

- I notice there is a pattern
- I notice the pattern is the

~~the~~ height times the number below it is the number of tiles

- I wonder if the "?" is 20?
- I wonder what we are doing with tiles?



# Abby

Look at this table. What do you notice? What do you wonder?

| Height | Number of Tiles |
|--------|-----------------|
| 1-2    | 2               |
| 2-3    | 6               |
| 3-4    | 12              |
| 4-5    | ? 20            |





# Joy

Is there a rule for this pattern? Can you write it out in words? Or in an equation?

$X = \text{Height}$

$Y = \text{\# of tiles}$

It is hard for me to write  
out in words but maybe  
an equation:

$$x(x+1) = y$$

# Abby

Is there a rule for this pattern? Can you write it out in words? Or in an equation?

Yes

Number  $\cdot$  (number + 1) = answer

$$X \cdot (x+1) = y$$



# Christine



# Christine



# How do you feel during math class?



**How do you like to show  
what you know and  
understand?**



**How can your teachers  
better understand what  
you know?**





# THANK YOU!

**ZACHARY CHAMPAGNE**

**zakchamp.com |  @zakchamp**

***zacharychampagne@gmail.com***